A NUMERICAL MODEL FOR MECHANICAL INTERACTION OF ROUGH SURFACES OF THE "PISTON-CYLINDER LINER" TRIBOSYSTEM

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Abstract: *The paper analyzes the numerical model of interaction of rough surfaces of the piston-cylinder liner tribosystem in the form of a Markov chain. It is based on a model that takes into account elastic and plastic deformation and fatigue failure under load. We have given a system of equations for the distribution of time-varying heights of protrusions. For contact interface of the piston-cylinder liner tribosystem of the diesel engine we analyzed the evolution of distributions.*

Keywords: piston-cylinder liner tribosystem, surface roughness, film thickness.

1. INTRODUCTION

Existing methods for calculating of friction characteristics are approximate and often inadequate for the engineer. Friction characteristics determined by such factors as surface micro geometry, physical characteristics of materials, velocity and the applied load. There is an approach based on the representation of the relief function for the random arguments [1,2]. Such models can estimate the area of contact, the friction force, coefficient of friction, wear, etc. However, this approach ignores the surfaces change and, consequently, contact and friction characteristics over the time. In this paper model of random change of surfaces heights over the time for "piston-cylinder liner" tribosystem is developed.

The "piston-cylinder liner" tribosystem is mostly in the hydrodynamic lubrication regime. At high loading levels, near the TDC, tribosystem is in the mixed or boundary lubrication regimes. The latter is important for the determination of the service life of the tribosystem as a whole.

2. DETERMINATION OF THE HYDROMECHANICAL CHARACTERISTICS OF THE "PISTON-CYLINDER LINER" TRIBOSYSTEM

The main hydromechanical characteristics (HMC) of the "piston-cylinder" tribosystem are: $h_{min}(\tau)$ – instantaneous values of the minimum oil film thickness; $p_{max}(\tau)$ – instantaneous values of the maximal hydrodynamic pressure; $h*_{min}$ – average value of $h_{min}(\tau)$; $p*_{max}$ – average value of $p_{max}(\tau)$; $N(\tau)$ and $N*$ – instantaneous and average power loss of friction; $Q*$ – the average flow rate of oil in the direction of the combustion chamber; $T*_{eff}$ – the average effective temperature of the lubricating layer.

Since the contact interaction of the elements is experimentally confirmed by the formation of "rubbing" on the piston skirt of diesel engine after certain hours (Fig. 1), the calculated characteristics of tribosystem complemented the areas, where minimal thickness of a lubricant film less than the permissible value $h_{lim} - \alpha_{h_{lim}}$ [%].
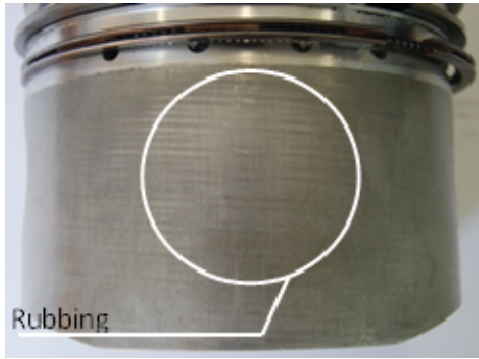
Figure 1. The result of contact interaction of the piston-cylinder liner interface

The reactions of the lubricating layer were determined based on the results of the numerical integration of the modified Elrod equation for pressure in the lubricating layer and the degree of filling of clearance [3]. The modified Elrod equation contains the function $\Omega(\varphi, \bar{z})$ and takes the form of:

$$\frac{\partial}{\partial \varphi}\left[\frac{\bar{h}^3}{12\bar{\mu}_{eff}^*}\frac{\partial}{\partial \varphi}(g\Omega)\right]+$$

$$+\frac{1}{a^2}\frac{\partial}{\partial \bar{z}}\left[\frac{\bar{h}^3}{12\bar{\mu}_{eff}^*}\frac{\partial}{\partial \bar{z}}(g\Omega)\right]= \quad (1)$$

$$=+\frac{\bar{w}}{2}\frac{\partial}{\partial \bar{z}}\left\{\bar{h}\left[1+(1-g)\Omega\right]\right\}+$$

$$+\frac{\partial}{\partial \tau}\left\{\bar{h}\left[1+(1-g)\Omega\right]\right\},$$

where $\bar{h} = h/h_0$; $\bar{\mu}_{eff}^* = \mu_{eff}^*/\mu_0$; $-a \leq \bar{z} \leq a$; $\bar{z} = z/R$; $\varphi = xR$; $a = B/2R$; $\tau = \omega_0 t$; $\bar{w} = w/(\omega_0 R)$; $\bar{h}$, $\bar{\mu}_{eff}$ – dimensionless film thickness and the effective viscosity of the lubricant; B, R – the width and radius of the bearing; μ_{eff}^* – effective viscosity of the lubricant, the corresponding temperature to T ; μ_0, h_0, ω_0 – respectively lubricant viscosity, typical film thickness at the center position of

the piston in cylinder and rotation speed of crankshaft; $\bar{w}$ – the dimensionless linear velocity of the piston; g – the switching function.

The function $\Omega(\varphi, \bar{z})$ is related to the degree of filling of the clearance $\theta(\varphi, \bar{z})$ and is characterized by a function that determines the mass content of the liquid phase (oil) in the volume of the clearance between the piston and cylinder using the relationship $\theta = 1 + (1-g)\cdot\Omega$.

For calculating the trajectory of the piston on the lubricating layer in the cylinder, the system of coordinates is fixed to a stationary cylinder. At the start, the origin of this moving coordinate system is at the center of mass (point C) of the moving piston (Fig. 2).
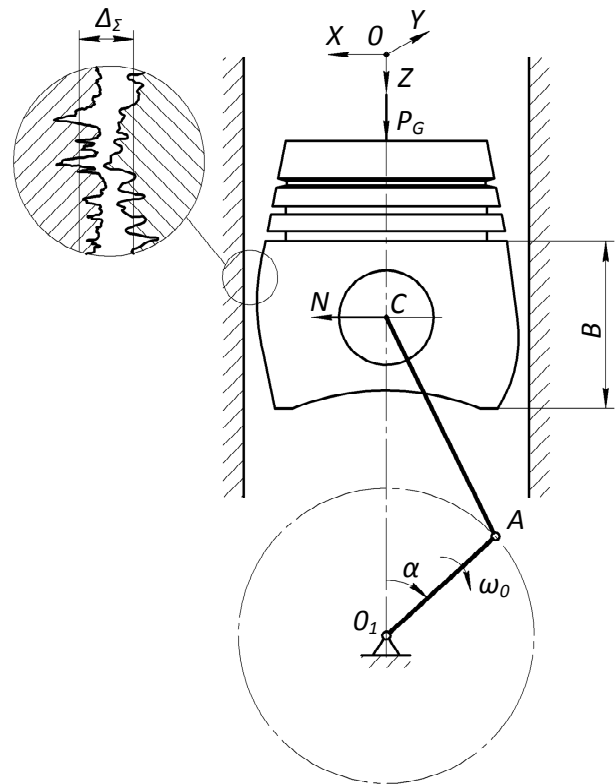
Figure 2. The scheme of the piston-cylinder liner interface

According to [4], it is assumed that movement of the piston in the cylinder is only in the plane perpendicular to the axis of the piston pin.

Given the initial data and the methodology for calculating the trajectory of piston's motion on the lubricating layer, as described in [5,6], we got the dependence of the minimum film thickness h_{min} in function of a crank angle α for a diesel engine (Fig. 3).
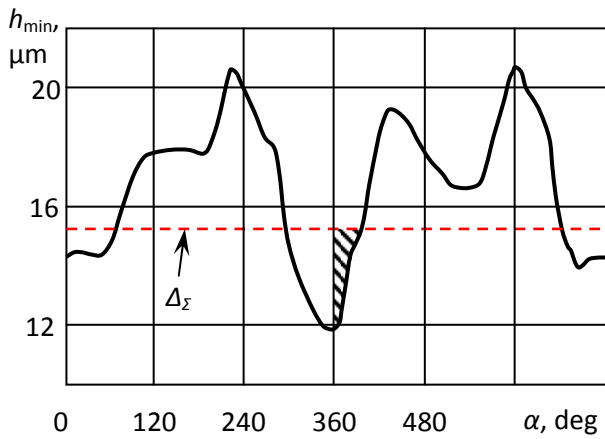
Figure 3. The minimal lubricant film thickness in function of the crankangle

The Figure 3 presents a dotted line area corresponding to working stroke, where the values of the h_{min} reach the values less than the total value of the sum of the maximum heights of microasperities (Δ_Σ) for the contact surfaces. In this moment of time the acting load (side force) increases and reaches 5000-7000 N [6]. The value of Δ_Σ was determined by recording profile traces of specimens of the piston and cylinder sleeve a Leica DCM 3D electron microscope and special software, which yielded the value of 15 μm.

For only the period of tribosystem's working time, where h_{min} less Δ_Σ (contact area, see. Fig. 3), we analyzed characteristics of the "piston-cylinder liner" tribosystem using Markov chains. Description of the used approach and model is below.

3. MARKOV CHAINS

To analyze the process of friction in the contact area we used the discontinuous model where surfaces are represented by asperities of random height (Fig. 4). Pairs of contacting asperities are changed when the shift occurs. Asperities in contact deform and destruct each other, that is why heights of contacting asperities may change. Total height change of all surface asperities leads to roughness transformations and variation of friction characteristics (real contact area, friction coefficient, wear).

Let's consider K pairs of asperities positioned in one raw. Time is discontinuous and is measured in shift counts. After n shifts

heights of asperities of one surface are represented by vector $\xi_k(n), (k = 1,...,K)$, and heights of asperities of the other surface are represented by vector $\eta_k(n)$. The asperity height change of the kth pair in one shift is described by general equations:

$$\xi_k(n+1) = \Psi(\xi_k(n), \eta_{k-1}(n)), \qquad (2)$$

$$\eta_k(n+1) = \Phi(\xi_k(n), \eta_{k-1}(n)), \qquad (3)$$

$$k = \overline{1,K}, \; \eta_0(n) = \eta_K(n),$$

where Φ and Ψ determine stochastic mechanism of asperity interaction as a sphere interaction [7], with random radiuses. Presented model of asperity interaction takes into account elastic-plastic deformation and wear.

Model is realized on a computer. After N shifts are performed, asperity height histogram is depicted, real contact area; friction force and wear are measured. Presented results agree to well known observations, such as independence of "equilibrium roughness" from initial surface roughness.

It is proposed to describe the trajectory of height changes of single asperity by means of Markov series, [8]. The height ξ of single asperity changes when it interacts with asperities of other surface, having heights $\eta(t)$ at the moment t. Time step Δt is selected in such a way, that values $\eta(t)$ and $\eta(t + \Delta t)$ are close to uncorrelated. It is supposed, that asperity with the height ξ interacts with the series of asperities of the other surfaces with heights $\eta_1,...\eta_n...$, distributed with density $q_n(y)$. Thus series of heights $\xi_1,...\xi_n...$ is obtained, height value ξ_{n+1} depends on ξ_n and η_{n+1}:

$$\xi_{n+1} = \Psi(\xi_n, \eta_{n+1}), \qquad (4)$$

where Ψ determines accepted mechanism of asperity contact interaction.

Series $\xi_1,...\xi_n...$ is Markov series. Moreover, heights $\xi_1,...\xi_n...$ are discontinuous, series $\xi_1,...\xi_n...$ becomes Markov chain. Similarly, ξ is distributed with density $p_\xi(x)$ and next equation is obtained:

$$\eta_{n+1} = \Psi(\xi_n, \eta_{n+1}). \qquad (5)$$
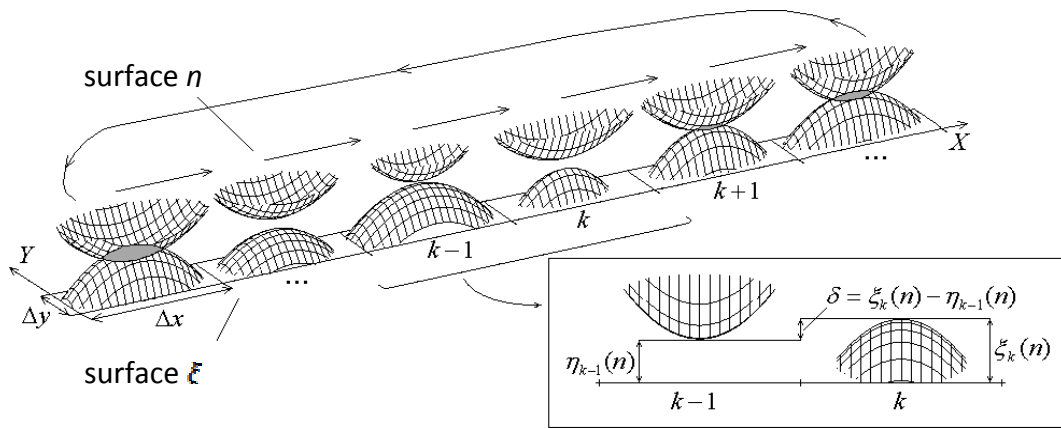
Figure 4. Model of surfaces and sketch of cyclical shifts

Once two functions Ψ and Φ are elaborated the system of equations for stationary distributions p^* and q^* is obtained:

$$\begin{cases} p^* = p^* \cdot P_\xi\left(q^*, \Psi\right), \\ q^* = q^* \cdot P_\eta\left(p^*, \Phi\right), \end{cases} \tag{6}$$

where $P_\xi\left(q^*, \Psi\right)$ and $P_\eta\left(p^*, \Phi\right)$ are matrices of transition probabilities for series of ξ_n and η_n. Elements of matrices are determined by distributions p^* and q^* – respondingly and by two functions Ψ and Φ. For example, elements of matrix $P_\xi\left(q^*, \Psi\right)$ is obtained:

$$\left\|P_\xi\right\|_{ij} = P\{\xi_{n+1} = j \mid \xi_n = i\} = \\ = \sum_{l:\Psi(i,l)=j} q^*(l). \tag{7}$$

Elements $P_\eta\left(p^*, \Phi\right)$ are determined similarly.

4. RESULTS AND DISCUSSION

Initial data were determined on base of recording profile traces of specimens of the piston skirt and cylinder liner [6]: the surface ξ is the surface of the cylinder liner, surface η – the surface of the piston skirt.

For period of time, where h_{min} less Δ_Σ we estimated next parameters: the distribution of the heights of roughness of surfaces (p_ξ, q_η); the root mean square deviations (rms) of surface roughness (σ_ξ, σ_η); the average contact area; the friction force F_{fr} and friction coefficient f; the linear wear l_h.

Figures 5a and b present the height distribution of surfaces in function of the friction distance. Changes of the surface (and consequently changes of the height distribution of the projections of the contact surfaces) due to fatigue failure is extremely slow, due to a low probability of this event. At the initial process of friction in contact come mostly high surface elements. The destruction of the high elements come into contact less high surface elements.
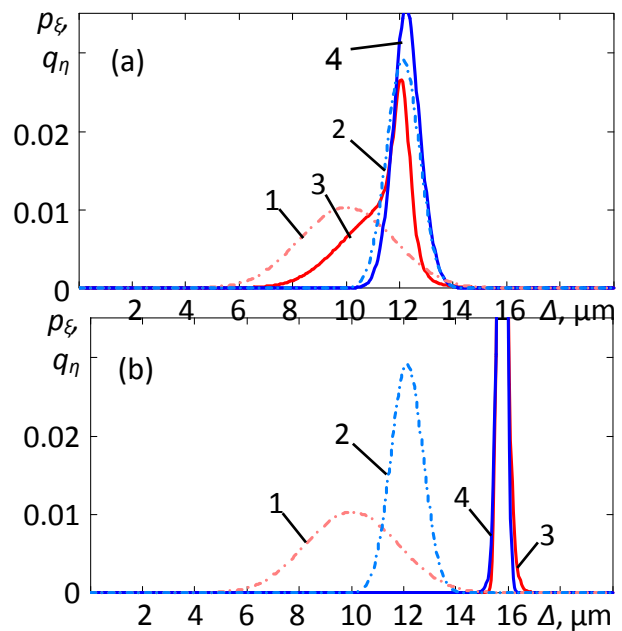

Figure 5. The distribution of the heights of roughness of contact surfaces for fiction distances 70 km (a) and 700 km (b); 1, 2 – initial curves for cylinder liner and piston respectively; 2, 3 – curves after interaction
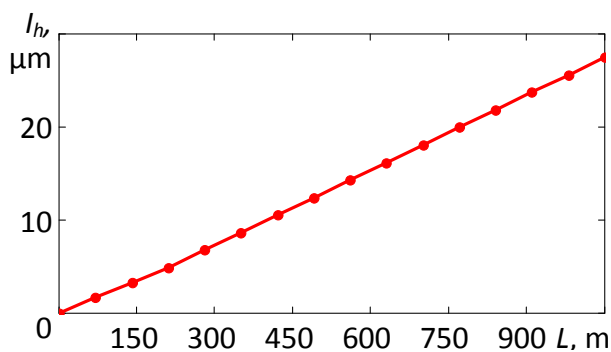
Under the influence of fatigue failure is a redistribution of the elements of heights, and in particular in the area of contact.

Figures 6a and 6b confirm the existence of "equilibrium roughness".

Figure 7 shows the dependence of wear on friction distance. Wear increased slowly.
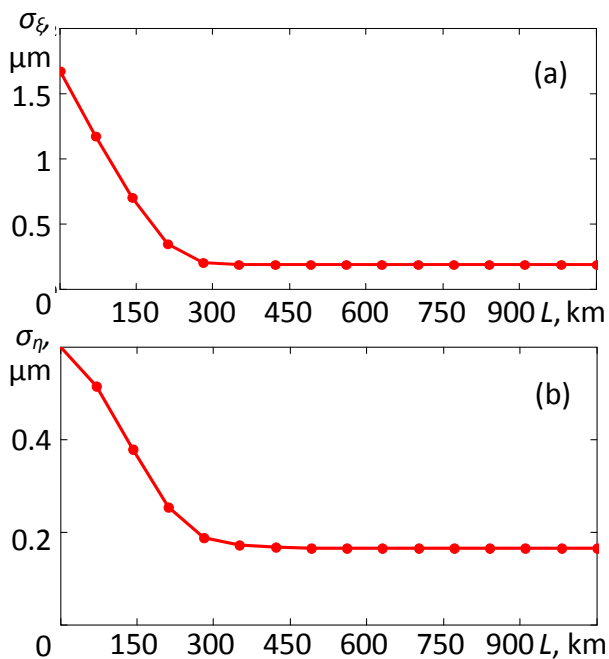
Figure 6. The rms of the heights of surface roughness of cylinder liner (a) and piston (b) in function of friction distance

Figure 7. The linear wear in function of friction distance

The increase of wear is connected with change of the height of the surfaces roughness under the influence of fatigue failure, as well as with the convergence of the interacting surfaces.

5. CONCLUSION

1. The HMC of the "piston-cylinder liner" tribosystem were calculated for diesel engine, which allowed us to estimate the duration of the surfaces contact interaction.
2. We proposed a Markov model of the interaction of rough surfaces, which allows to estimate the friction characteristics over the time for contact area of "piston-cylinder liner" tribosystem.
3. Estimations agree with experimental observations.

REFERENCES

[1] P.R. Nayak: Random process model of rough surfaces, Journal of Lubrication Technology, pp. 398-407, 1971.

[2] J.A. Greenwood, J.B.P. Williamson: Contact of nominally flat surfaces, Proceedings of Royal Society, Series A, Vol. 295, pp. 300-319, 1966.

[3] V.N. Prokopiev, A.K. Boyarshinova, K.V. Gavrilov: Hydromechanical characteristics heavy-loaded bearings including non-round pins and bushings, Problems of mechanical engineering and reliability of the machines, No. 5, pp. 98-104, 2009 [in Russian].

[4] Y.V. Rojdestvensky, K.V. Gavrilov, A.A. Doikin: Solving of optimization task for tribological piston and rotor machines by using the mass conservation algorithm, Friction and lubrication in machines and mechanisms, No. 8, pp. 38-43, 2011 [in Russian].

[5] V.N. Prokopiev, Yu.V. Rozhdestvenskii, N.V. Shirobokov: Increasing of effectiveness of algorithms of outlet parameters of in a complicated manner loaded sliding supports of transport machines engines, Vestnik Ural. Mezhregion. Otd. Ross. Akad. Transporta, No. 2, pp. 28, 1999 [in Russian].

[6] I.G. Goryacheva, A.V. Morozov, Y.V. Rozhdestvensky, K.V. Gavrilov, A.A. Doikin: Development of method for calculating and experimentally evaluating tribological parameters of piston-cylinder tribosystem of diesel engine, Journal of Friction and Wear, Vol. 34, No. 5, pp. 339-348, 2013.

[7] K.L. Johnson: *Contact Mechanics*, Cambridge University Press, 1987.

[8] J.L. Doob: *Stohastic Processes*, Jonh Willey & Sons, New York, 1953.